

Applied Problem

2.) In the problem this is what they gave me: $a = \text{acceleration}$, $J = a'(t)$
↑ Jerk

a) Jerk is the derivative of acceleration

b.) $s(t) = -8.25t^2 + 66t$ $a'(t) = J$

$$s'(t) = 2(-8.25)t + 66$$

$$s''(t) = -16.5$$

The double derivative of $s(t)$ is -16.5 .

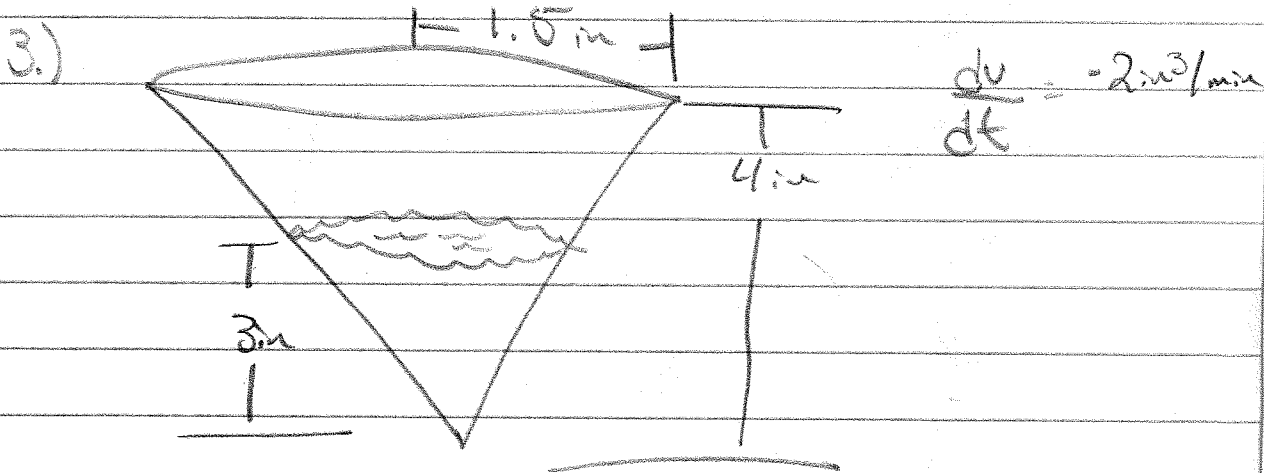
C.) "a" equals position

"b" equals acceleration

"c" equals Jerk

"d" equals velocity

line a is the position, line b is the acceleration, c is Jerk and d is the velocity.



I was given the diameter of cone is 3m, the height is 4m and that the new height of water level is 3m. Also I was given rate of change of water volume is $-2 \text{ m}^3/\text{min}$.



$$V = \frac{\pi}{3} r^2 h$$

$$\frac{1.5}{4} = \frac{r}{h}$$

$$\frac{r}{1.5} = \frac{h}{4}$$

$$4r = 1.5h$$

$$r = 3.75(h)$$

$$r = \frac{3}{2}h$$

$$r = \frac{3}{8}h$$

$$V = \frac{\pi}{3} \left(\frac{3}{8}h \right)^2 \cdot h$$

$$V = \frac{\pi}{3} \cdot 140625 h^3$$

$$\frac{dV}{dt} = 3(\pi \cdot 046875) h^2 \frac{dh}{dt}$$

$$\frac{dV}{dt} = 3(9)(0.046875\pi) \frac{dh}{dt}$$

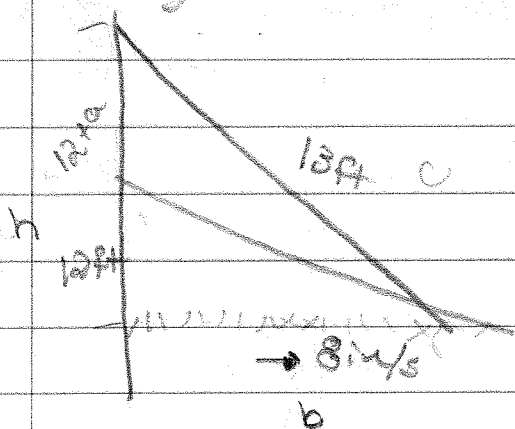
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$$1.265625$$

$$\frac{dh}{dt} = -0.503 \text{ in/min}$$

The height of the water in the cone changed at a rate of -0.503 in/min

6.) In Problem 6 I was given: $\frac{db}{dt} = 8 \text{ in/s}$
length of ladder is 13 ft.



Formula for Area of triangle $\frac{1}{2}bh$

$$\text{given } \frac{db}{dt} = 8 \text{ in/sec}$$

$$\text{gip. } \frac{18A}{12\pi r} = \frac{8}{12} = \frac{2}{3}$$

have to find $\frac{dA}{dt}$ when $r=12$

$$A = \frac{1}{2}bh$$

$$h = \sqrt{169 - b^2}$$

$$b = \sqrt{169 - h^2}$$

$$A = \frac{1}{2}b(\sqrt{169 - b^2})$$

$$b = 5$$

$$\frac{dA}{dt} = \frac{1}{2} \left[\frac{1}{\sqrt{169 - b^2}} (-2b \frac{db}{dt})(b) + (\sqrt{169 - b^2}) \left(\frac{db}{dt} \right) \right]$$

$$\frac{-b^2}{\sqrt{169 - b^2}} \cdot \frac{db}{dt} + \sqrt{169 - b^2} \frac{db}{dt}$$

$$\frac{dA}{dt} = \frac{1}{2} \frac{db}{dt} \left[\frac{-b^2}{\sqrt{169 - b^2}} + \sqrt{169 - b^2} \right]$$

$$\frac{dA}{dt} = \frac{1}{2} \cdot 8 \cdot \left[\frac{-25}{12} + 12 \right]$$

$$\frac{dA}{dt} = 3.305 \text{ in}^2/\text{s}$$

